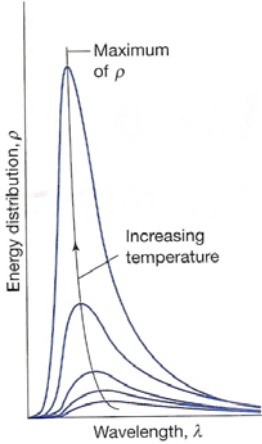


Minimum requirements for **underneath of your pillow**. However, **write your own summary!** You need to know the story behind the equations...

The summary is not necessarily directly related to your exams. I may ask you to explain concepts rather than memorizing equations. However, you have to know some of them.

**Be aware of typos.**

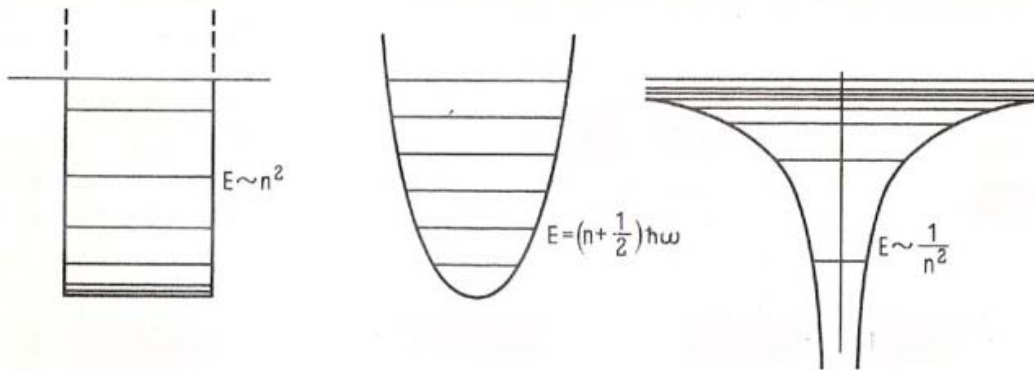
## CLASSIC EXPERIMENTS

<p><b>Blackbody radiation</b></p> 	$E = nh\nu; n = 0, 1, 2, 3, \dots$ <p>Which led to:</p> $R(\lambda) = \frac{2\pi hc}{\lambda^5} \frac{1}{e^{hc/\lambda kT} - 1}$ $T\lambda_{\max} = \text{const} \quad \text{Wien's displacement law}$ $E_{\text{tot}} = \int_0^{\infty} R(\lambda) d\lambda \approx T^4 \quad \text{Stefan-Boltzmann's law}$
<p><b>Photoelectric effect</b></p> <p>Experimental results:          threshold frequency <math>\nu_0</math>  <math>\nu_0</math> depends on substance          light intensity <math>\sim</math> # of photoelectrons  <math>E_{\text{kin}}</math> independent of light intensity</p>	<div data-bbox="932 1194 1330 1409"> <p><b>Quantization of light</b></p> <math display="block">E_{\text{photon}} = h\nu</math> <p>particle – wave duality</p> </div> <div data-bbox="932 1430 1330 1623"> <p><b>Photoelectric effect</b></p> <math display="block">E_{\text{kin}} = h\nu - \phi</math> </div>

## Emission/absorption spectra & Bohr's model

$$\bar{\nu} = \frac{1}{\lambda} = R_{\infty} \left( \frac{1}{n'^2} - \frac{1}{n^2} \right)$$

### “Simple potentials” and the corresponding eigenvalues



## Particle in a 1D box

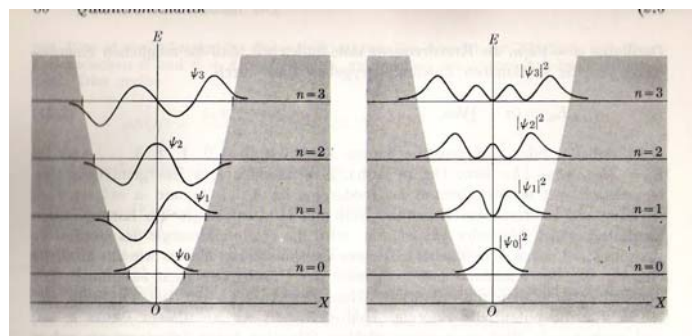
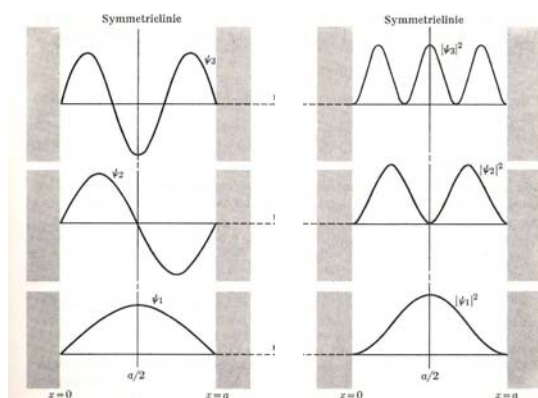
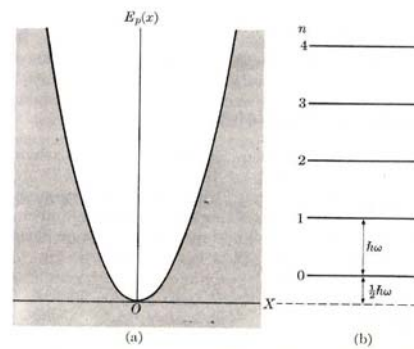
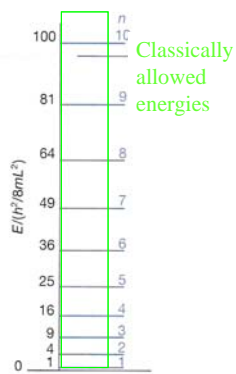
$$|\psi|^2 = \frac{2}{a} \sin^2\left(\frac{n\pi x}{a}\right)$$

$$E = \frac{h^2}{8ma} n^2 \approx n^2$$

$$E_0 = E(n=1)$$

## Harmonic oscillator

Look it up & write your own summary



<b>wave functions</b> $\Psi = \Psi(x_1, y_1, z_1, x_2, y_2, z_2, \dots, t)$ $= \Psi(\vec{r}_i, t)$ $= e^{-iEt/\hbar} \psi(\vec{r})$ $\psi = \psi(x_1, y_1, z_1, x_2, y_2, z_2, \dots) = \psi(\vec{r}_i)$	<b>probabilities</b> $P = \int  \Psi ^2 d\tau$
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## SCHRÖDINGER EQUATION

$$-\frac{\hbar}{i} \frac{\partial \Psi}{\partial t} = -\frac{\hbar^2}{2m_i} \frac{\partial^2 \Psi}{\partial x_i^2} + V\Psi \quad (\text{time dependent})$$

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \psi(x)}{\partial x^2} + V(x)\psi(x) = E\psi(x) \quad (\text{time independent})$$

with operators

$$\hat{H} \equiv -\frac{\hbar^2}{2m} \nabla^2 + V \quad (\text{Hamilton operator})$$

$$-\frac{\hbar}{i} \frac{\partial \Psi}{\partial t} = \hat{H}\Psi \quad (\text{time dependent}) \quad \hat{H}\psi = E\psi \quad (\text{time independent})$$

<b>Eigenvalues</b> The possible results in a measurement of a physical/chemical quantity are the Eigenvalues of the corresponding observable.	$\hat{M}\Psi = c\Psi$ ; $\Psi$ is Eigenfunction of the operator $\hat{M}$ with Eigenvalue $c$ .
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Averaging

... what was this all about ?

## OPERATORS

observable		operator	
name	symbol	symbol	operation
position	x	$\hat{X}$	multiply by x
momentum	$p_x$	$\hat{p}_x$	$-i\hbar \frac{\partial}{\partial x}$
kinetic energy	$K_x$	$\hat{K}_x$	$-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2}$
potential energy	V(x)		
total energy	E		
angular momentum	$L_x = y p_z - z p_y$		

## Approximation methods

### Variation theorem

The true ground state energy, i.e., the eigenvalue of the time-independent Hamilton operator  $\hat{H}$  of a quantum-mechanical system obeys

$$\frac{\int \phi^* \hat{H} \phi d\tau}{\int \phi^* \phi d\tau} \geq E_{gr,true}$$